# Luminosity Estimate in a Multi-TeV Muon Collider Using $e^+e^- \rightarrow \mu^+\mu^-$ as the Muon Source

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## **Basic Method**

- 1. Annihilate high energy positrons and atomic electrons in the reaction,  $e^+e^- \rightarrow \mu^+\mu^-$ , to produce low emittance muon beams for injection into a multi-TeV muon storage ring. The fixed target threshold is a 43.7 GeV positron beam to produce two muons at rest in the CM.
- 2. Look at thin material targets because of much larger electron densities compared to a plasma. Because of beam degradation, the target has an effective length which is a function of the track length (TL) of positrons which remain above the threshold.
- 3. Calculate the # of muons/positron by integrating over energy,

#
$$\mu$$
/e<sup>+</sup> =  $\int e^{-}/cm^{3} \cdot TL(E) \cdot \sigma(E) dE$ 

4. To achieve the lowest possible muon emittance try to make sure, as much as possible, that it will only be determined by the positron beam size and the maximum muon production angle.

#### **Some Previous Work on this Subject:**

1. D. Kaplan, P. Allport, T. Hart, <a href="http://arxiv.org/pdf/0707.1546.pdf">http://arxiv.org/pdf/0707.1546.pdf</a>

"Producing an Intense, Cool Muon beam via e<sup>+</sup>e<sup>-</sup> Annihilation</sup>", Nov. 2006

Looked at ways to get the required muon rate of 10<sup>13</sup> – 10<sup>14</sup> /sec by boosting the positron beam current. Discussed colliding beams, high-power targets, e<sup>+</sup> storage ring, e<sup>-</sup> gun, e<sup>+</sup> ERL.

Concluded that "given the extraordinary beam and target parameters required, the cost effectiveness is far from clear".

2. M. Antonelli, P. Raimondi, INFN-13-22/LNF and Snowmass 2013 Report

"Ideas for Muon Production from Positron Beam Interaction on a Plasma Target"

Considered a plasma electron density of 10<sup>20</sup> e<sup>-</sup>/cm<sup>3</sup> and a plasma length of 10 m.

Discussed the production cross section and beam degradation due to radiative

Bhabha scattering. Muon production rate near threshold from an SLC –type machine

~0.5 x 10<sup>6</sup>/sec. Try for very low emittance.

Now try looking at thin material targets to see if smaller emittance could make up for many orders of magnitude in lower muon production rate compared to a proton source.

#### **Choice of Positron Beam Energy**

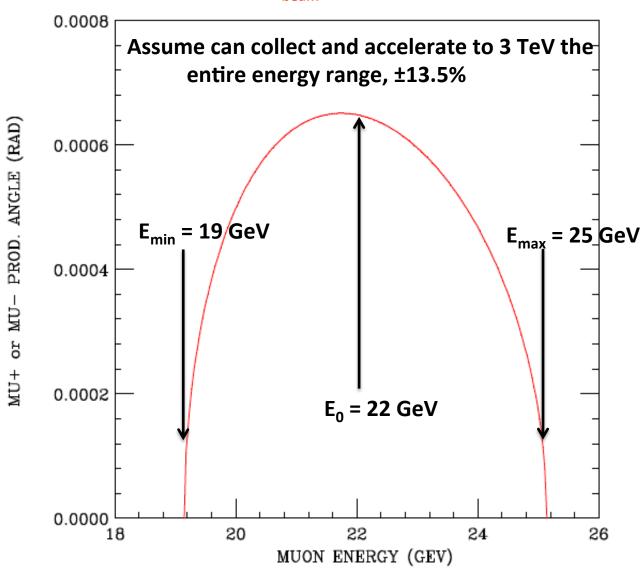
- 1. Consider 3 TeV muon beams with energy spread ±0.1% at the IP (same as the MAP White paper at Snowmass 2013).
- 2. Starting with a muon central energy,  $E_0 = 22$  GeV, take the muon source energy spread to be  $\delta = (3000/22)(\pm 0.1\%) = \pm 13.5\%$ . Assume this can be captured and damps linearly, so the source energy range becomes:

$$19 < E_{\mu} < 25 \text{ GeV}$$

3. A 44.5 GeV positron beam produces muons that completely cover this energy range.

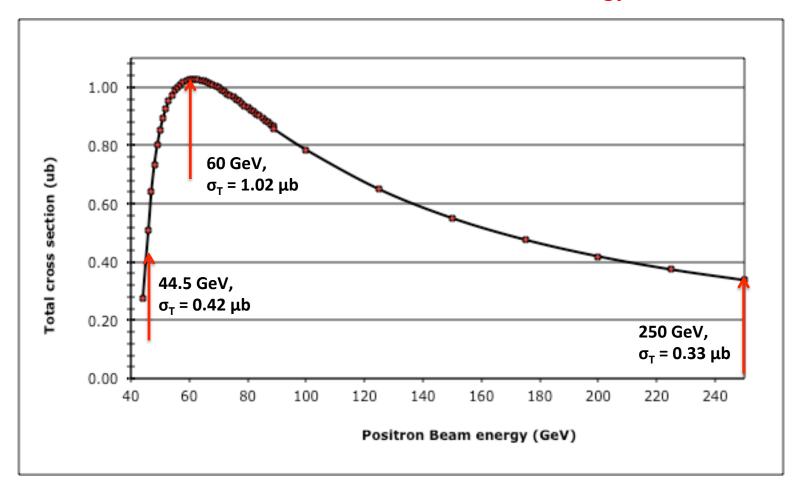
## **Production Kinematics**

#### **Muon Production Angle vs. Muon Energy**



## Positron Fixed Target Cross Section, $e^+e^- \rightarrow \mu^+\mu^-$

#### **Total Annihilation Cross Section vs. Beam Energy**



Positron beam energy > 44.5 GeV only results in increasing muon production outside the usable energy range, negating the increase in total cross section.

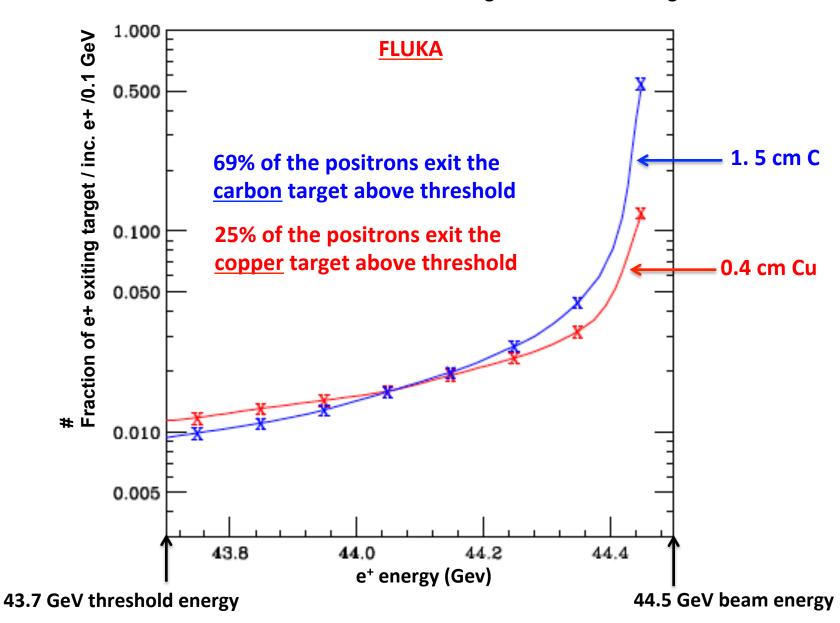
## **Target Choice**

- For a positron beam near the muon production threshold the target thickness is limited by beam degradation from radiative Bhabha scattering,  $e^+e^- \rightarrow e^+e^- \gamma$  and bremsstrahlung.
- For areal electron density, ρt ≥ 10<sup>24</sup> e<sup>-</sup>/cm<sup>2</sup>, and beam energy near production threshold a substantial fraction of the beam positrons begin to fall below threshold. For a given ρt, low Z targets have smaller radiation length and therefore limit beam degradation from bremsstrahlung next slide.
- For ~1 radiation length targets the muon production is dominated by the twostage Bethe-Heitler process,  $e^+ \rightarrow \gamma \rightarrow \mu^+ \mu^-$ , which gives a much larger angular spread as well as more MCS.

In summary, after trying C, Ti, Cu, and W, ended up choosing 1.5 cm of carbon (0.08 rl and  $\rho t = 10^{24} e^{-}/cm^{2}$ ).

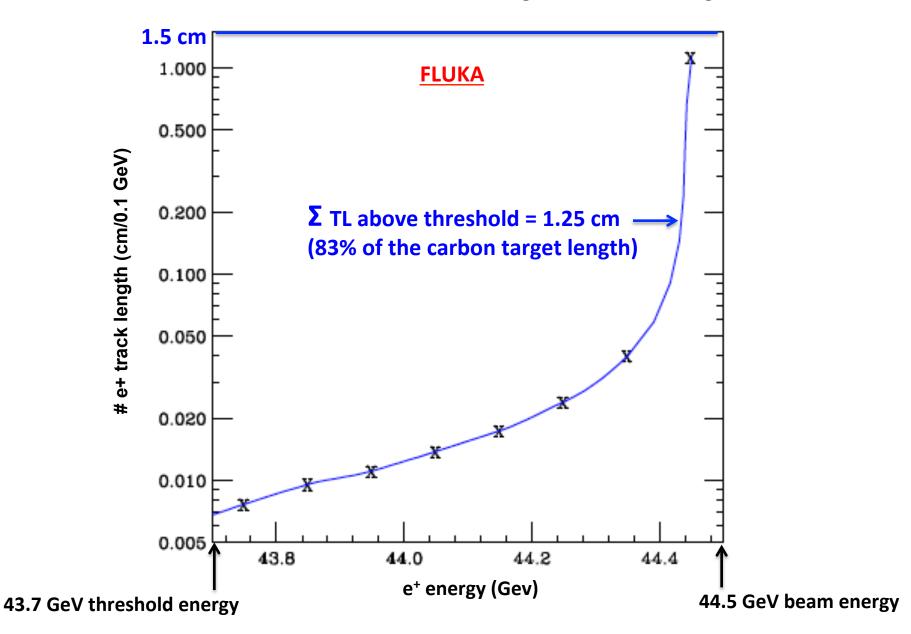
#### Beam Degradation in Carbon and Copper Targets ( $\rho t = 10^{24} e^{-}/cm^{2}$ )

**Includes Radiative Bhabha Scattering and Bremsstrahlung** 



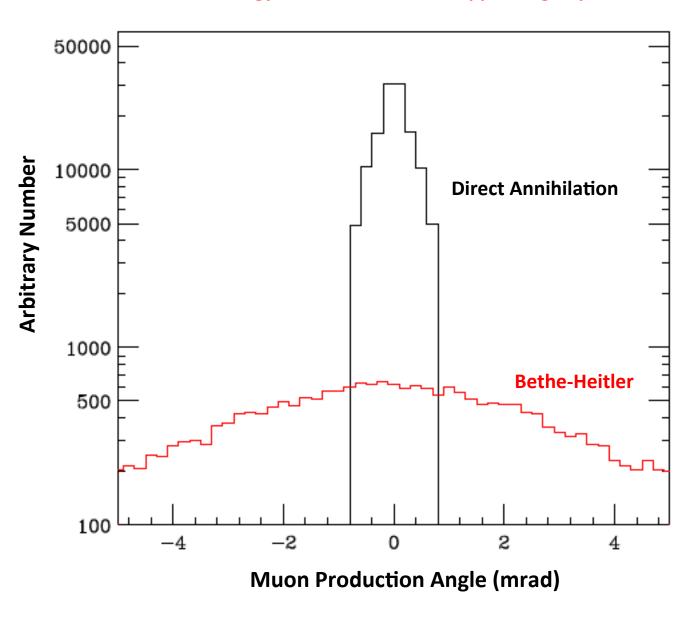
### Positron Beam Track Length (TL) above Threshold for a 1.5 cm Carbon Target

Includes radiative Bhabha scattering and bremsstrahlung



### **Angular Distribution for Direct Annihilation and Bethe-Heitler Production**

Positron Beam Energy = 44.5 GeV, 0.4 cm copper target,  $\rho t = 10^{24} e^{-}/cm^{2}$ 



## **Muon Beam Emittance**

Start with the ILC positron beam parameters, 2.6 x  $10^{14}$  /sec in 10 bunch trains (41µA), scaled to a round spot at 44.5 Gev:

$$\sigma_x = \sigma_v = 0.5\mu$$
,  $\sigma_{x'} = \sigma_{v'} = 50 \mu rad$ ,  $\sigma_L = 0.25 mm$ 

Muon kinematics give the <u>polar</u> angle,  $\theta_{max}$  = 0.65 mrad, which will be increased by the angular spread of the positron beam, MCS of the incoming positron beam, and MCS of the outgoing muons. Taking half of the maximum angle and including MCS gives a divergence (non-Gaussian) = 0.31 mrad in each plane.

The effective source size is given by the positron beam size but has to also include a contribution MCS of the incoming beam and from the production angle extended over the length of the target. This gives an effective source size of 0.9µ.

Multiplying by muon  $\gamma_{22~GeV}$  gives a normalized emittance,  $\epsilon_x$  =  $\epsilon_y$  = 5.7 x 10<sup>-5</sup>  $\pi$  mm-rad

## **Results for 6 TeV CM**

	<u>Proton Source</u>	e <sup>+</sup> e <sup>-</sup> Source
Muon rate	2.4 x 10 <sup>13</sup> /sec	9.5 x 10 <sup>7</sup> /sec
Muons/bunch	2 x 10 <sup>12</sup>	9.5 x 10 <sup>6</sup>
δ	0.1%	0.1%
$\gamma \epsilon_{_{TN}}$	25x10 <sup>-6</sup> πm	5.7x10 <sup>-8</sup> πm
γε <sub>ιΝ</sub>	0.07 πm	0.007 πm
β*	0.005 m	0.00025 m
$\sigma_{x}^{*} = \sigma_{v}^{*}$	1.5 μ	0.022 μ
$\sigma_{x'}^* = \sigma_{y'}^*$	420 μrad	90 μrad
$\sigma_{L}^*$	0.0025 m	0.00025 m
Luminosity	8.8 x 10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup>	1.4 x 10 <sup>28</sup> cm <sup>-2</sup> s <sup>-1</sup>

## **Summary and Comments**

- 1. Because of the relatively large divergence in muon production angles, even near threshold, could only get about a factor of 450 reduction in normalized emittance compared to the proton source design, and cutting on the production angle costs cross section linearly.
- 2. If compared to the MAP Higgs Factory design, the emittance reduction factor becomes about 7,000, but the requirement of a very small energy spread severely limits the fraction of usable muon production cross section.
- 3. The obvious way to achieve a luminosity comparable to the proton source design is to increase the positron beam current by a factor (8.8 x  $10^{34}/1.4$  x  $10^{28}$ )  $^{1/2}$   $\approx$  2,500, so 41  $\mu$ A => 100 mA. An ERL might be an option, but is beyond current technology.
- 4. To achieve  $\rho t = 10^{24} e^{-}/cm^{2}$  in plasma would need either a very long plasma or a series of short plasmas with optics in between to control the effective source size (Raimondi).
- 5. Survival of the 15 mm carbon target has not been addressed here, but simple dE/dx shows that at 100 mA, 500 kW is deposited in the carbon alone.
- 6. The SLC parameters at 44.5 GeV scaled to Higgs factory energy with 0.1% energy spread give a luminosity of 1.8 x 10<sup>16</sup> cm<sup>-2</sup>s<sup>-1</sup>.

We conclude that, even with the substantial emittance reduction estimated here, significant developments would be needed to reach the proton source luminosity design in a TeV class muon collider.